

## Single function machines

INPUT  $\rightarrow$   $\rightarrow$  OUTPUT

The number that goes IN The number that comes out

This box gives the calculation instruction

To find the input from the output  
Use the **INVERSE** operation

## Using letters to represent numbers

|  |                 |                                     |
|--|-----------------|-------------------------------------|
| $5 + 5 + 5$  | $y + y + y + y$ | $20 - h$                            |
| $3 \times 5$   | $y \times 4$    | $\frac{20}{h}$                      |
| $5 \times 3$   | $4 \times y$    | $\uparrow$                          |
|  | $4y$            | $\uparrow$                          |
| Addition and multiplication can be done in any order | 4 lots of 'y'   | 20 shared into 'h' number of groups |
| <b>Commutative calculations</b>                      |                 |                                     |

## Single function machines (algebra)

INPUT  $\rightarrow$   $\rightarrow$  OUTPUT

$a \rightarrow 10a$   
 $3c \rightarrow 30c$

$\leftarrow -10$

To find the input from the output  
Use the **INVERSE** operation

## Find functions from expressions

INPUT  $7x \rightarrow$   $\rightarrow$  OUTPUT  $14x$

Find the relationship between the input and the output

Sometimes there can be a number of possible functions.  
e.g.  $+7x$  or  $\times 2$  could both be solutions to the above function machine

## Substitution into expressions

$4y \leftarrow$  4 lots of 'y'

If  $y = 7$  this means the expression is asking for 4 'lots of' 7

$4 \times 7$  OR  $7 + 7 + 7 + 7$  OR  $7 \times 4$   $= 28$

e.g.:  $y - 2$   
 $= 7 - 2 = 5$

## Two step function machines

INPUT  $\rightarrow$   $\rightarrow$   $\rightarrow$  OUTPUT

Calculate the value at the end of each operation

For the input use the **INVERSE** operations

## Two step function machines (algebra)

$b \rightarrow$   $\xrightarrow{5b}$   $\rightarrow 5b + 4$

$\leftarrow +5$        $\leftarrow -4$

**IMPORTANT** Calculate the value at the end of each operation

$c \rightarrow$   $\xrightarrow{c+4}$   $\rightarrow 5(c + 4)$

$\leftarrow -4$        $\leftarrow +5$

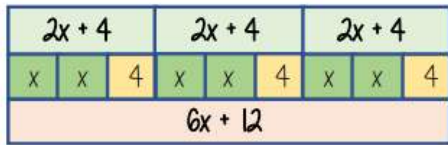
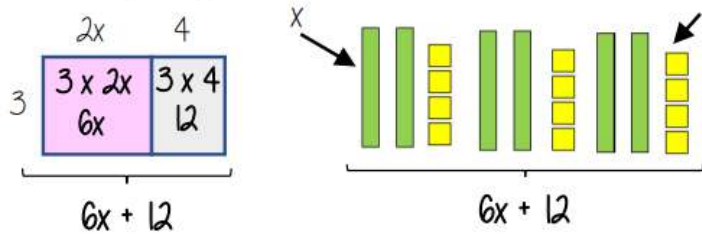
**NOTE:** The whole first output is multiplied by 5  
 $= 5c + 20$

## Formulae and Equations

Formulae – all expressed in symbols  $\xrightarrow{\text{Substitute in values}}$  Equations – include numbers and can be solved

## Multiply single brackets

$$3(2x + 4)$$



Different representations of  $3(2x+4) = 6x + 12$

## Equations with unknown on both sides

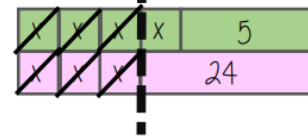
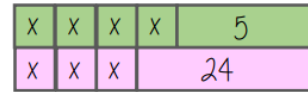
$$4x + 5 = 3x + 24$$

$$-3x \quad -3x$$

$$x + 5 = 24$$

$$-5 \quad -5$$

$$x = 19$$



## Keywords

**Inverse:** the operation that undoes what was done by the previous operation. (The opposite operation)

**Commutative:** the order of the operations do not matter.

**Substitute:** replace one variable with a number or new variable.

**Evaluate:** work out

**Simplify:** grouping and combining similar terms

**Equivalent:** something of equal value

**Coefficient:** a number used to multiply a variable

**Solve:** find a numerical value that satisfies an equation

## Algebraic constructs

### Expression

A sentence with a minimum of two numbers and one maths operation

### Equation

A statement that two things are equal

### Term

A single number or variable

### Identity

An equation where both sides have variables that cause the same answer includes  $\equiv$

### Formula

A rule written with all mathematical symbols e.g. area of a rectangle.  $A = b \times h$

## Solve equations with brackets

**R**

$$3(2x + 4) = 30$$

Expand the brackets

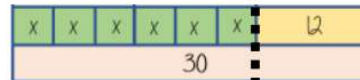
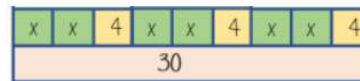
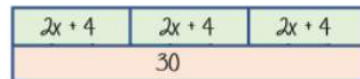
$$6x + 12 = 30$$

$$-12 \quad -12$$

$$6x = 18$$

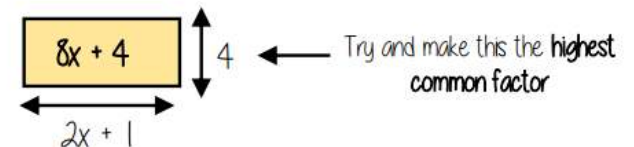
$$+6 \quad +6$$

$$x = 3$$



## Factorise into a single bracket

$$8x + 4$$



The two values **multiply** together (also the area) of the rectangle

$$8x + 4 \equiv 4(2x + 1)$$

Note:

$$8x + 4 \equiv 2(4x + 2)$$

This is factorised but the HCF has not been used